How does one compute the interquartile range, ie the difference between the 25<sup>th</sup> percentile and 75<sup>th</sup> percentile for a given normal distribution with known mean and variance? Well, it is actually very straightforward and the process is detailed as follows:



Let the  $25^{\text{th}}$  and  $75^{\text{th}}$  percentiles be *a* and *b* respectively.

Then  $P(X < a) = 0.25 \Rightarrow a = invNorm(0.25, \mu, \sigma)^*$ and  $P(X < b) = 0.75 \Rightarrow b = invNorm(0.75, \mu, \sigma)^*$ As such, IQR = Q3 - Q1 = b - a

\*These cited are mere graphic calculator commands; alternatively you may consult a standard normal distribution table to arrive at *a* and *b*.

For normal curves specifically **centered about the vertical axis**, owing to symmetry, the interquartile range is simply twice that of the 75<sup>th</sup> percentile,

ie 
$$IQR = Q3 - Q1 = 2Q_3$$

Adding on, did you also know that **the interquartile range for a normal distribution is approximately 1.35 times its standard deviation**? Let's see how this is true.

Once again, we establish that P(X < a) = 0.25 and P(X < b) = 0.75

Standardizing X to the random variable Z for both equations,

$$P\left(Z < \frac{a-\mu}{\sigma}\right) = 0.25 \qquad P\left(Z < \frac{b-\mu}{\sigma}\right) = 0.75$$
$$\frac{a-\mu}{\sigma} = invNorm(0.25) = -0.675 \qquad \frac{b-\mu}{\sigma} = invNorm(0.75) = 0.675$$
$$a = -0.675\sigma + \mu - - - - -(1) \qquad b = 0.675\sigma + \mu - - - - -(2)$$

Subtracting (1) from (2) therefore yields  $b - a = IQR = 1.35\sigma$  (shown)